

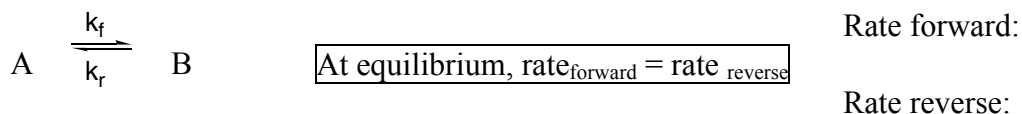
Ch. 16 Chemical Equilibrium

16.1 Characteristics of a System at Chemical Equilibrium

- Not completely on product or reactant side – have some of each
 - “product favored” equilibrium– more product
 - “reactant favored” – mostly reactant
- “Dynamic Equilibrium”
 - forward rate = reverse rate
 - reactions happen, but cancel each other out, so that no overall change
 - “steady state” = “equilibrium”
 - It may seem like nothing is changing or happening, but is molecular action (“dynamic”)
- Previous Examples
 - Vapor Pressure (closed container) Liquid \rightleftharpoons vapor
 - Saturated solution solid \rightleftharpoons dissolved
 - Weak acid/weak electrolyte HF \rightleftharpoons H⁺ + F[⊖]
- In achieving an equilibrium it doesn't matter whether you start from left side or right side
 - Either way, you end up with the same balance between reactants and products once equilibrium has been established
 - Figure 14.1 Moore, Fig T-117, 118 Brown

The Equilibrium “Constant”

A. Intro



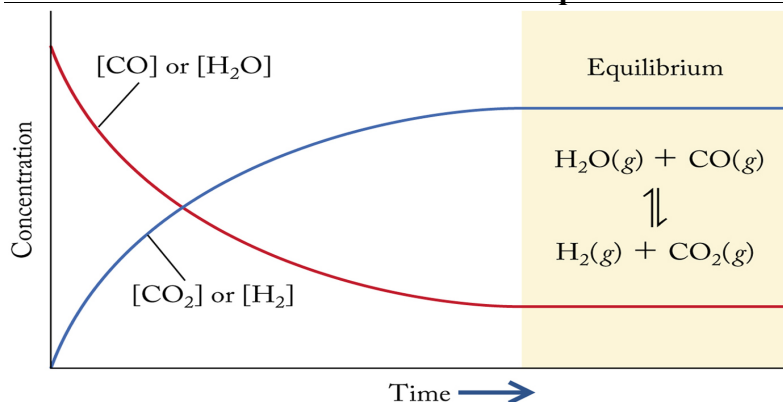
Equality:

 K_c

Rearrange:

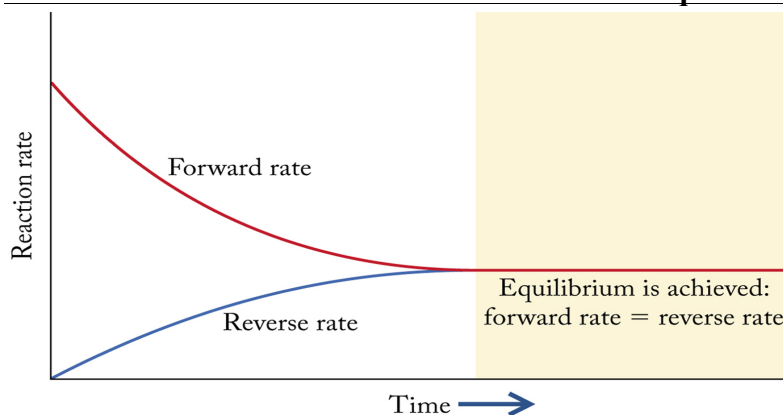
Notes

- K_c is a constant
- Each reaction has its own unique “K” constant
 - called the “EQUILIBRIUM CONSTANT”
- Ratio of **product over reactant**
 - concentrations are used** in “M” (Molarity) = mole/liter
- For gases, a K_p constant based on gas pressures can also be used. **(16.3)**
 - I'll do molarity ones for test problems and home-made problems. But the setup logic is the same for gas problems, in book or online homework or whatever.

Amounts of materials before and after equilibrium is Achieved:

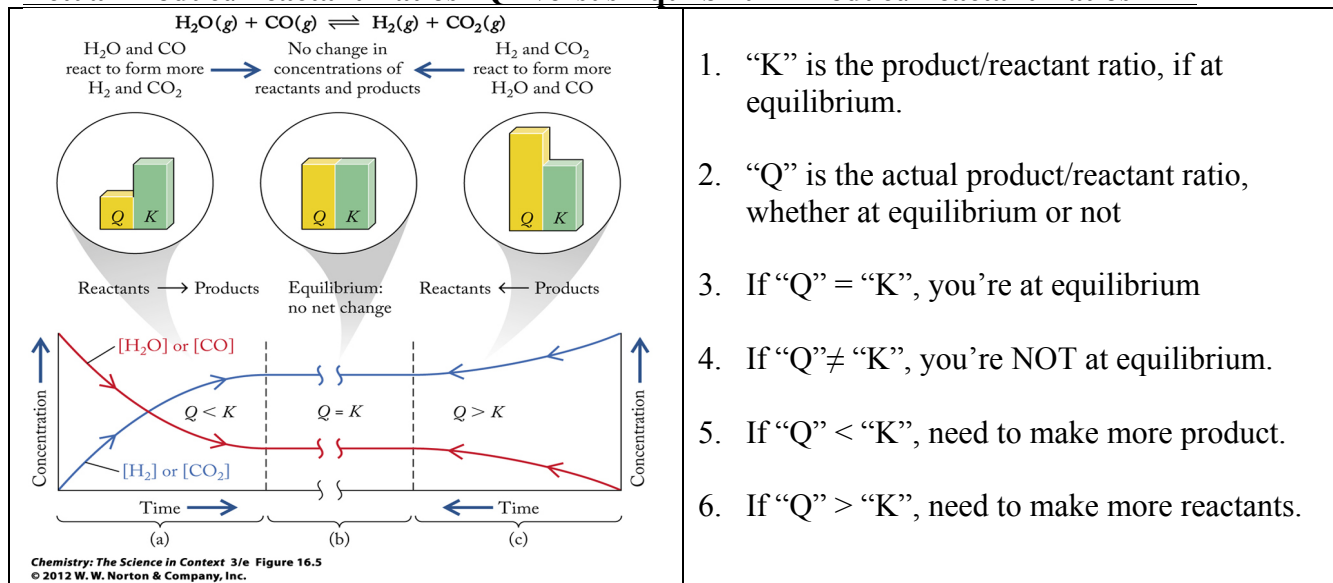
Chemistry: The Science in Context 3/e Figure 16.1
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1. At equilibrium, amounts stay constant.
2. Prior to equilibrium amounts were changing.

Forward and Reverse Rates Prior to and After Equilibrium is Achieved:

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1. At equilibrium, rates are equal
2. Prior to equilibrium, rates were not equal.

Actual Product/Reactant Ratios “Q” versus Equilibrium Product/Reactant Ratios “K”

1. “K” is the product/reactant ratio, if at equilibrium.
2. “Q” is the actual product/reactant ratio, whether at equilibrium or not
3. If “Q” = “K”, you’re at equilibrium
4. If “Q” \neq “K”, you’re NOT at equilibrium.
5. If “Q” < “K”, need to make more product.
6. If “Q” > “K”, need to make more reactants.

B. Qualitative things the value of K tells us:

- At equilibrium, is the product favored or the reactant?
 - $K \gg 1 \rightarrow$ product favored
 - $K \ll 1 \rightarrow$ reactant favored

Concept Problem: $A \rightleftharpoons B$ Find $[B]/[A]$ ratios if:

a. $K_c = 10^3$

b. $K_c = 10^{-3}$

- If the **actual** initial ratio **Q** does not equal the equilibrium ratio **K**, in which direction will reaction go to achieve equilibrium? (In other words, if you start out not at equilibrium, how will the system respond to get to equilibrium?) (**Section 16.5**)
 - If actual ratio “Q” < K, the product/reactant ratio will need to increase in order to reach the target “K”
 - Practical:
 - If actual ratio “Q” > K, the product/reactant ratio will need to decrease in order to reach the target “K”
 - Practical:

Concept Problem: $A \rightleftharpoons B$ $K_c = 0.20$ How will $[A]$ and $[B]$ change/respond to reach equilibrium (which will go up and which will get down?) if initial conditions are:

a. $[A] = 0.20 \text{ M}$ and $[B] = 0.00 \text{ M}$

b. $[A] = 0.10 \text{ M}$ and $[B] = 0.50 \text{ M}$

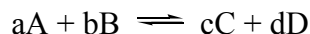
- What will specific concentrations be at equilibrium?
 - If you know K and other information, you can solve for all the equilibrium concentrations

Concept Problem: $A \rightleftharpoons B$ $K_c = 0.20$

a. If the system is at equilibrium and $[A] = 0.10 \text{ M}$, what must be $[B]$?

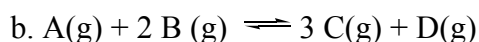
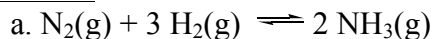
b. If the system is at equilibrium and $[B] = 0.10 \text{ M}$, what must be $[A]$?

c. If the system is **not** at equilibrium, and the initial scenario has $[B] = 0.60 \text{ M}$, what will be the concentrations after equilibrium is achieved?

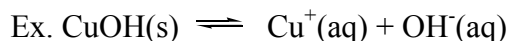
Writing K expressions: General (16.2)

$$K_c = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$


1. Products over reactants
2. To the “coefficient” power
3. Straight from the balanced equation
 - don’t need mechanism, etc.
 - Not like a rate law where equation doesn’t really tell you anything

Write K_c Expressions**Heterogeneous Equilibria (16.6):** Do not include solids or liquids (solvents) in K expressions

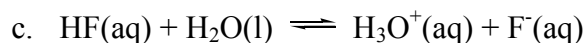
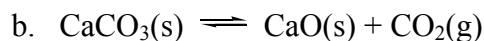
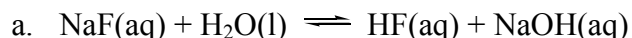
- The concentrations of solids and liquids (solvents) are constant, so just wrap into K
- only gases and “aqueous things” (solutes) appear in K expressions
 - these are things whose concentrations are **not** constant
 - A(g), B(aq) Yes
 - C(l), D(s) No
- When water is involved as either a reactant or a product, it does **not** appear in the K expression (when the reaction takes place in aqueous solvent)



$$K_1 = \frac{[Cu^+][OH^-]}{[CuOH]} \quad \text{so} \quad K_2 = [Cu^+][OH^-]$$

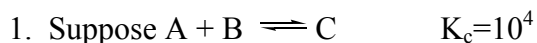


Constant

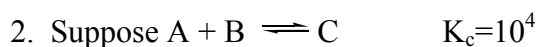
Write K Expressions

Manipulating Equilibrium Constant Expressions. K's for Related Reactions. (16.4)

- When a reaction is written in the reverse direction, the K value is inverted
 - $K_{\text{reverse}} = 1/K_{\text{forward}}$
- When the coefficients for a reaction are doubled or halved, the K value ends up being squared or “square rooted”



What is K for $C \rightleftharpoons A + B$
(Draw both the expression and the actual K value)



What is K for $2A + 2B \rightleftharpoons 2C$
(Draw both the expression and the actual K value)

16.3 Calculating K values

- Key: You need all equilibrium concentrations. Then you can plug into K expression and solve.

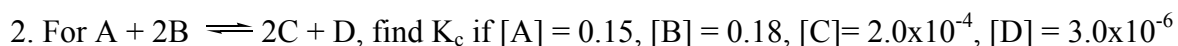
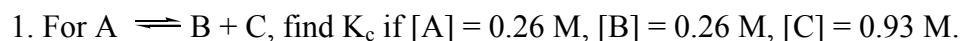
Two ways to know all the equilibrium concentrations.

1. You are simply given all of the equilibrium concentrations. (easy)
2. You are given all of the **initial** concentrations, and **at least one final concentration**, but then must use the “ICE” (**I**nitial-**C**hange-**E**quilibrium) method to figure out what they would all be at equilibrium (harder)

A. Given all of the Equilibrium concentrations, solve for K (easy)

Solution steps:

- a. Based on the balanced reaction, write out the correct K expression
- b. Enter the known concentrations values and solve for K



B. Given all of the **initial** concentrations, and **at least one final concentration**, solve for K (harder) (16.8).

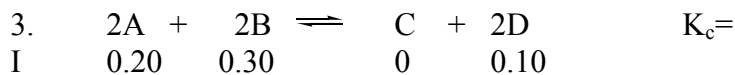
Solution steps:

- Based on the balanced reaction, write out the correct K expression
- Use the “ICE” (**I**nitial-**C**hange-**E**quilibrium) method to figure out the equilibrium concentrations
- Enter the equilibrium concentration values and solve for K

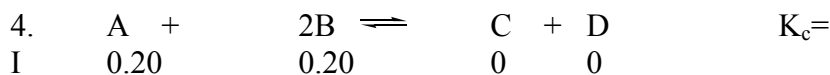
Using the “ICE” Method to Calculate K, Given Initial Concentrations and One Final Concentration

- Write balanced equation, and expression for K_c
- Make an “ICE” table, and enter the knowns
 - Initial
 - Change
 - Equilibrium
- Find the Change for the chemical whose final concentration is known
- Use stoichiometric relationship to determine the change in concentrations for the others
- From the initial concentrations and the deduced changes, determine all equilibrium concentrations
- With all equilibrium concentrations now known, plug into the K_c expression and solve for K
- Check: Does Answer Make Any Sense?
 - Note: equilibrium concentrations must be in Molarity, moles/liter. If information is given in grams or moles plus solvent volume, you will need to convert into molarity.

Use the ICE method to find the equilibrium concentrations and the K values for the following:



C



C



Chemical Meaning of K

- $K_c \gg 1$ Product Favored
 - $K_c \ll 1$ Reactant Favored
 - $K_c \approx 1$ Significant quantities of both products and reactants---calculations required
- There are many cases where $K_c \ll 1$, but small amount of product are still very important.

Some more Uses for K Values**A. Predicting the direction of a reaction, given information about actual situation. (16.5 Equilibrium Constants K and Reaction Quotients Q)**

K=equilibrium Q=actual ratios (same format)

- If $Q=K$, you're at equilibrium. The situation won't change
- If $Q<K$, you're not at equilibrium. You are short on product, so reactions will go to products to achieve equilibrium. Shift from left to right.
- If $Q>K$, you're not at equilibrium. You have excess product, so products will go to reactants to achieve equilibrium. Shift from right to left.

1. $A + B \rightleftharpoons C$ $K_c = 72$
Suppose [A], [B], and [C] all begin at 0.33 M:

- What is Q?
- Which direction will the reaction go to achieve equilibrium?
- What will happen to the concentrations of: (will they go up or down?)

[A] [B] [C]

B. Calculating Equilibrium Concentrations, Given K and Some Other Information (16.8, 2)

1. If all but one equilibrium concentration is given: (easy, plug and chug...)

Solution steps:

- Based on the balanced reaction, write out the correct K expression
- Enter the known K and the known concentrations values and solve for the unknown concentration

Example. $HF(aq) \rightleftharpoons H^+(aq) + F^-(aq)$ $K_c = 6.8 \times 10^{-4}$

a. Find $[H^+]$ if $[HF] = 0.10$ and $[F^-] = 0.10$.

b. Find $[F^-]$ if $[HF] = 0.20$ and $[H^+] = 10^{-3}$.

2. If K number and initial concentrations are given, but no equilibrium concentrations are given, use ICE to calculate the equilibrium concentrations.

Using the “ICE” Method to Calculate Equilibrium Concentrations, Given Only Initial Concentrations and K_c

1. Write balanced equation, and expression for K_c
2. Make an “ICE” table, and enter the known initial concentrations
 - a. Initial
 - b. Change
 - c. Equilibrium
3. Use “ x ” to define the change of one substance.
4. Use stoichiometric relationships to determine the changes in the concentrations for the others, in terms of “ x ”.
5. Calculate the equilibrium concentrations of all chemicals in terms of initial concentrations and “ x ”, and enter them in the table.
 - Ex: $0.30 - x$, or $0.30 - 2x$, or $0.00 + x$, or $0.00 + 2x$
 - **If K is small** so that “ x ” is likely to be small, **use the simplifying assumption** that $[A]_{\text{initial}} - “x” = [A]_{\text{initial}}$
 - This is often justified, and can greatly simplify the math.
 - Ex: $0.20 - x = 0.20$ if x is smaller than 0.01
6. Solve for “ x ” (This is the hard part!)
7. **Once “ x ” is known, use it to solve for the actual equilibrium concentrations**
8. Check: Does Answer Make Any Sense?
9. Check: If you made the “simplifying assumption”, was it justified? (Was “ x ” $< 5\%$ of $[A]_{\text{initial}}$?)

Note: Some hard math!! Quadratics are tedious!

- If possible, being able to avoid needing to solve quadratics saves a lot of time (and mistakes)

***Great simplifying assumption (avoids a lot of quadratics):**

1. changes “ x ” are often small
 - For something with nonzero original concentration, the change “ x ” in concentration is often so small that it doesn’t significantly change the original concentration
 - $[\text{original concentration}] - “x” (\text{change in concentration}) = [\text{original concentration}]$
2. Useful strategy:
 - a. Make the simplifying assumption
 - b. Check at end whether “ x ” $> 5\%$ of the original concentration
 - If not, the simplifying assumption is pretty good
 - If yes, the simplifying assumption is not valid and leads to some nontrivial error. In which case you need to go back and solve completely (often involving quadratic or perhaps even worse).

Concept Example: Why is the Simplifying Assumption Often Justifiable? $0.20 - x = ???$

<u>If "x" =</u>	<u>Then $0.20 - x =$</u>	<u>After roudoff to 2 sig. fig.</u>	<u>Is simplifying assumption valid?</u>
2×10^{-7}	$0.20 - 0.0000002 =$		
2×10^{-6}	$0.20 - 0.000002 =$		
2×10^{-5}	$0.20 - 0.00002 =$		
2×10^{-4}	$0.20 - 0.0002 =$		
2×10^{-3}	$0.20 - 0.002 =$		
2×10^{-2}	$0.20 - 0.02 =$		

-Check at end. If $x > 5\%$ of number, the assumption causes trouble.

Problems

1. If 0.10 mol of N_2O_4 is added to 1L flask, what will be the concentrations at equilibrium?

Quadratic Required. K too large to justify simplification $N_2O_4 \rightleftharpoons 2NO_2$ $K = 0.211$

InitialChangeEquilibrium**Equilibrium:**

$[N_2O_4]$

$[NO_2]$

2. Find final concentrations:

Initial Concentrations

0.20 0 0

ChangeEquilibriumEquilibrium withSimplifying Assumption

Equilibrium:

$[HA]$

$[H^+]$

$[A^-]$

3. Find final concentrations given:



Initial 0.30

Change

Equilibrium

**Equilibrium with
Simplifying Assumption**

Equilibrium:

4. Find final concentrations given:



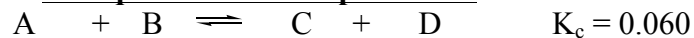
Initial 0.30

Change

Equilibrium

Equilibrium:

5. Find final concentrations given: **A “Square Root” Simplification**

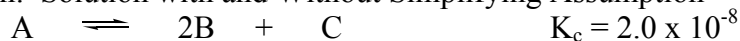


Initial 0.30 0.30

Change

Equilibrium

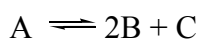
6. Find final concentrations given: Solution with and Without Simplifying Assumption

**Initial** 0.20**Change****Equilibrium****Equilibrium with****Simplifying Assumption**

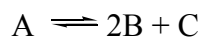
With Simplifying Assumption

Without Simplifying Assumption

Solution With and Without Simplifying Assumption:



$$K_c = 2.0 \times 10^{-8}$$



<p>With I</p> <table style="border-collapse: collapse;"> <tr><td style="padding-right: 10px;">0.20</td><td style="padding-right: 10px;">0</td><td>0</td></tr> <tr><td style="padding-right: 10px;">C</td><td style="padding-right: 10px;">-x</td><td>2x</td></tr> <tr><td style="padding-right: 10px;">E</td><td style="padding-right: 10px;">.20-x</td><td>2x</td></tr> <tr><td style="padding-right: 10px;">E*</td><td style="padding-right: 10px;">0.20</td><td>x</td></tr> </table> <p>So $K = 2.0 \times 10^{-8} = \frac{(2x)^2 x}{0.20} = \frac{4x^3}{.20}$</p> <p>$0.4 \times 10^{-8} = 4x^3$ Easy $x^3 = 1.0 \times 10^{-9}$ x = 1.0 x 10⁻³</p>	0.20	0	0	C	-x	2x	E	.20-x	2x	E*	0.20	x	<p>Without (using .20 - x for [A] at eq)</p> $K = 2.0 \times 10^{-8} = \frac{(2x)^2 x}{0.20 - x}$ <p>So $2.0 \times 10^{-8} (0.20 - x) = 4x^3$</p> <p>So $4.0 \times 10^{-9} - 2.0 \times 10^{-8} x = 4x^3$</p> <p>So $4x^3 + 2.0 \times 10^{-8} x - 4.0 \times 10^{-9} = 0$ Not Easy!!!</p>
0.20	0	0											
C	-x	2x											
E	.20-x	2x											
E*	0.20	x											

16.7 How Systems Respond When an Equilibrium is Disturbed. LeChatelier's Principle.

1. At Equilibrium, there is a steady state of concentrations.
2. How does a system respond when an equilibrium is disturbed?

Le Chatelier's Principle: when a system is disturbed from equilibrium, it responds so as to reduce or counteract the effect of the change.

1. A revised equilibrium gets reestablished
 - a. Usually the same K value must still apply
 - unless the temperature is changed
 - b. But different actual concentrations result
 - whether you added or subtracted a reactant, a product, some solvent, or the volume
2. The reaction can move in the forward direction (more reactants go to product side) or the reverse direction (more products go back to starting materials) as needed to offset a change

Qual: If something extra is added, react from that side toward the other to remove some of it
 If something is removed, react from the other side to replace it

LeChateliers's Principle: Summary

A change in any of the factors that determine the equilibrium conditions of a system will cause the system to change in such a manner as to reduce or counteract the effect of the change.

Factor that Changes	Direction of the Change	Direction to Restore Equilibrium
1. Concentration	↑ Reactant	Forward
	↑ Product	Reverse
2. Temperature	↑ T, when $\Delta H > 0$	Forward – K increases
	↑ T, when $\Delta H < 0$	Reverse – K decreases
3. Volume	↑ V, when $\Delta n_{\text{gas}} > 0$	Forward
	↑ V, when $\Delta n_{\text{gas}} = 0$	No effect
A change in volume impacts gas pressure. An increase in volume reduces pressure.	↑ V, when $\Delta n_{\text{gas}} < 0$	Reverse

If you reverse any of the Changes above, the **Direction to reach Equilibrium** reverses

3 Factors That can Be Changed 1) Concentrations 2) Temperature 3) Volume (which impacts gas pressure)	Goals 1) restore $Q = K$ 2) offset change
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LeChatelier's Principle: Response to Disrupted Equilibria

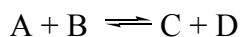
$$\Delta H < 0 \text{ (exothermic)}$$

TABLE 16.4 Responses of an Exothermic Reaction [2 A(g) ⇌ B(g)] at Equilibrium to Different Kinds of Stress		
Kind of Stress	How Stress Is Relieved	Direction of Shift
Add A	Remove A	To the right
Remove A	Add A	To the left
Remove B	Add B	To the right
Add B	Remove B	To the left
Increase temperature by adding heat	Consume some of the heat	To the left
Decrease temperature by removing heat	Generate heat	To the right
Increase pressure by compressing the reaction mixture	Reduce moles of gas to relieve pressure increase	To the right
Decrease pressure by expanding volume	Increase moles of gas to maintain equilibrium pressure	To the left

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A. Concentration Change: Addition or Removal of Either a Reactant or a Product

1. If you add (or remove) a chem, at that moment $Q \neq K$
2. The system (and concentrations) will shift forward or backward to adjust Q so $Q = K$
 - **NOTE: K value does not change**
 - many chemical ways to remove a chem (precipitations, acid-base, etc.)

Example

Disruption	Immediate Impact on Q	Direction to Restore Eq	Response (following disruption) :			
			[A]	[B]	[C]	[D]
Add A	$Q < K$	Forward	↓	↓	↑	↑
Add B						
Add C						
Add D						
Remove A						
Remove B						
Remove C						
Remove D						

B. Volume Change: Only Relevant When Gases are Involved

1. When the volume changes, it causes a change in concentrations
 - at the instant of change $Q \neq K$
 - note: the actual K value is unchanged

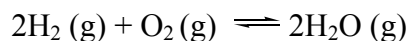
2. Qualitative sense:

- a. **When the volume expands, you want to generate more gas molecules to fill it**
- b. **When the volume shrinks, you want to get rid of gas molecules so it isn't too full**

3. Volume changes will only matter if one side of the equation has more gas on it than the other
 - if moles of gas are equal on both sides, volume changes have no impact

<u>Disruption</u>	<u>Response</u>
Volume Increase	Shift toward side with more gas
Volume Decrease	Shift toward side with less gas

4. Volume and Pressure: A different qualitative way to understand why a system will respond
 - When the volume expands, pressure decreases
 - a. When the volume expands and the pressure drops, you want to generate more gas molecules to fill the container and restore pressure
 - b. When the volume shrinks, you want to get rid of gas molecules to unclutter the container and to restore the original pressure

Volume Example

<u>Volume Change</u>	<u>Direction to Restore Eq</u>	Response of moles of: $2\text{H}_2(\text{g}) + \text{O}_2(\text{g}) \rightleftharpoons 2\text{H}_2\text{O}$
Increase		
Decrease		

C. Temperature Change

1. View heat as either a reactant or a product

- $\Delta H > 0$ Endothermic Heat is required, on Reactant Side
- $\Delta H < 0$ Exothermic Heat is produced, on Product Side

2. When the temperature rises, the system responds so as to remove extra heat

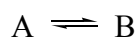
3. When the temperature drops, the system responds so as to replace missing heat

4. When the system shifts to the right or to the left in response to a temperature change, this means that chemical concentrations change, too

5. A Temperature Changes Causes a Changes in the K Value

- Because the Product/Reactant Ratio Changes
 - $\Delta H > 0$ Rise in temp \rightarrow shift to right \rightarrow K rises
 - $\Delta H > 0$ Drop in temp \rightarrow shift to left \rightarrow K drops
 - $\Delta H < 0$ Rise in temp \rightarrow shift to left \rightarrow K drops
 - $\Delta H < 0$ Drop in temp \rightarrow shift to right \rightarrow K rises

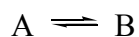
1. Write in "heat" as reactant or product, and predict the responses when temperature changes:



$$\Delta H < 0$$

<u>Temperature Change</u>	<u>Direction to Restore Eq</u>	Response of moles of: $\text{A} \rightleftharpoons \text{B}$	Response of K Value
Increase			
Decrease			

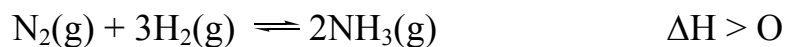
2. Write in "heat" as reactant or product, and predict the responses when temperature changes:



$$\Delta H > 0$$

<u>Temperature Change</u>	<u>Direction to Restore Eq</u>	Response of moles of: $\text{A} \rightleftharpoons \text{B}$	Response of K Value
Increase			
Decrease			

3. Write in “heat” as reactant or product, and predict the responses to the changes:



<u>Disruption</u>	<u>Direction to Restore Eq</u>	Response of moles of: $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$	Response of K Value
1. Temperature Increase			
2. Volume Increase			
3. Added N_2			
4. Removal of NH_3			
5. Reduced temperature			
6. Added NH_3			
7. Removal of N_2			
8. Volume reduction			

D. Addition Catalyst: Equilibrium is reached faster, but the actual K value or equilibrium product/reactant ratios are unchanged.

Some Math Tips: CHEMICAL EQUILIBRIA Chem 210-Jasperse Ch. 16

1. $(a + b)^2 = a^2 + 2ab + b^2$

example: $(0.24 - x)^2 = 0.0576 - 0.48x + x^2 = x^2 - 0.48x + 0.0576$

example: $(3.2e-5 - x)^2 = 1.02e-9 - 6.4e-5 x + x^2 = x^2 - 6.4e-5 x + 1.02e-9$

2. Quadratic Equation: $ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

example: $x^2 - 1.48x + 0.0576 = 0$ $x = 1.44$ or 0.04

example: $x^2 - .60x + 0.025 = 0$ $x = 0.43$ or 0.17

Note 1: Quadratics are a bother to solve. Avoid them if possible. Often the “simplifying assumption” (see #4) can enable you to avoid quadratic solutions.

Note 2: Quadratics can often give 2 answers, but one will frequently be nonsense.

3. “SIMPLIFYING ASSUMPTION”: If $m \gg x$, then $m - x = m$ (approximately)

examples: $0.14 - 3.6e-5 = 0.14$

$1.23e-3 - 1.0e-6 = 1.23e-3$

Use: for many equations in which K is small, “x” will also be relatively small. In these circumstances, the degree to which the starting materials react (“x”) will be relatively insignificant from their concentrations perspective, and we can assume the equilibrium concentration of the reactants will not differ significantly from their initial concentration.

- THE SIMPLIFYING ASSUMPTION WILL OFTEN MAKE THE USE OF THE QUADRATIC EQUATION UNNEEDED
- Guide: If “x” is >5% of “m”, then the simplifying assumption is not appropriate.

4. The “Square Root” Simplification: If both numerator and denominator have “squares”, it is convenient to take the square root of both sides to simplify

examples: $0.10 = x^2 / (0.050 - x)^2$ Take square root of both sides: $0.316 = x / (0.050 - x)$

Rearrange: $0.0158 - 0.316x = x$

Solve for “x”: $x = 0.012$

5. $m = x^n$

To solve for x, when “m” and “n” are known:

- enter “m”
- hit $x^{1/y}$ or $\sqrt[n]{\quad}$ button (depending on your calculator)
- enter “n”

example:

$25 = x^3$ $x = 2.92$

$1.48e-6 = x^3$ $x = 0.0114$

$2.14e-13 = x^4$ $x = 6.80e-4$

Using the “ICE” Method to Calculate K, Given Initial Concentrations and One Final Concentration

1. Write balanced equation, and expression for K_c
2. Make an “ICE” table, and enter the knowns
 - a. Initial
 - b. Change
 - c. Equilibrium
3. Find the Change for the chemical whose final concentration is known
4. Use stoichiometric relationship to determine the change in concentrations for the others
5. From the initial concentrations and the deduced changes, determine all equilibrium concentrations
6. With all equilibrium concentrations now known, plug into the K_c expression and solve for K
7. Check: Does Answer Make Any Sense?
 - Note: equilibrium concentrations must be in Molarity, moles/liter. If information is given in grams or moles plus solvent volume, you will need to convert into molarity.

Using the “ICE” Method to Calculate Equilibrium Concentrations, Given Only Initial Concentrations and K_c

1. Write balanced equation, and expression for K_c
2. Make an “ICE” table, and enter the known initial concentrations
 - a. Initial
 - b. Change
 - c. Equilibrium
3. Use “x” to define the change of one substance.
4. Use stoichiometric relationships to determine the changes in the concentrations for the others, in terms of “x”.
5. Calculate the equilibrium concentrations of all chemicals in terms of initial concentrations and “x”, and enter them in the table.
 - Ex: $0.30 - x$, or $0.30 - 2x$, or $0.00 + x$, or $0.00 + 2x$
 - **If K is small** so that “x” is likely to be small, **use the simplifying assumption** that $[A]_{\text{initial}} - “x” = [A]_{\text{initial}}$
 - This is often justified, and can greatly simplify the math.
 - Ex: $0.20 - x = 0.20$ if x is smaller than 0.01
6. Solve for “x” (This is the hard part!)
7. **Once “x” is known, use it to solve for the actual equilibrium concentrations**
8. Check: Does Answer Make Any Sense?
9. Check: If you made the “simplifying assumption”, was it justified? (Was “x” < 5% of $[A]_{\text{initial}}$?)

LeChateliers's Principle: Summary

A change in any of the factors that determine the equilibrium conditions of a system will cause the system to change in such a manner as to reduce or counteract the effect of the change.

Factor that Changes	Direction of the Change	Direction to Restore Equilibrium
1. Concentration	↑ Reactant	Forward
	↑ Product	Reverse
2. Temperature	↑ T, when $\Delta H > 0$	Forward – K increases
	↑ T, when $\Delta H < 0$	Reverse – K decreases
3. Volume	↑ V, when $\Delta n_{\text{gas}} > 0$	Forward
	↑ V, when $\Delta n_{\text{gas}} = 0$	No effect
A change in volume impacts gas pressure. An increase in volume reduces pressure.	↑ V, when $\Delta n_{\text{gas}} < 0$	Reverse

If you reverse any of the Changes above, the **Direction to reach Equilibrium** reverses

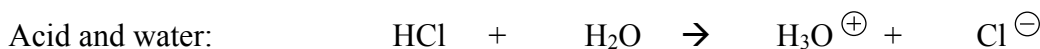
Ch. 17 Acids and Bases

Acid/base character (pH) of a solution has enormous impact

- lake biosystem (acid rain)
- farming/gardening (soil pH, alkalinity, etc)
- rusting/corrosion
- biology
 - cells, proteins, blood, enzymes, hormones need very tight pH control
 - Most bio reaction mechanisms involve H^+ transfer $\rightarrow [H^+]$ has huge impact on rates

17.1 Bronsted-Lowry Concept of Acids/Bases

	Bronsted-Lowry Definition	<u>Lewis Definition</u>
Acid	H^+ donor	Lone-pair acceptor
Base	H^+ acceptor	Lone-pair donor

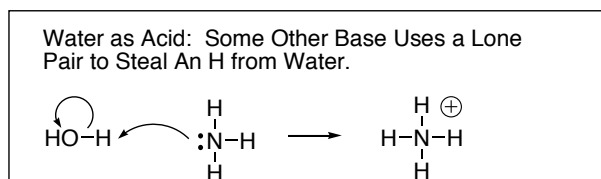
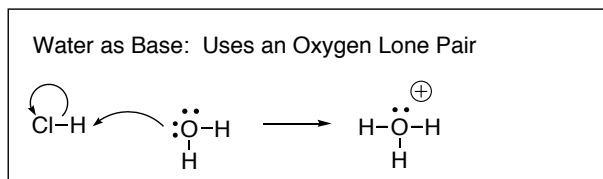


Notes:

- An **acid loses** an H^+ and gets more negative
 - A neutral acid becomes an **anion** after loss of H^+ $HCl \rightarrow Cl^-$
 - A cationic acid becomes neutral after loss of H^+ $H_3O^+ \rightarrow H_2O$
- A **base gains** an H^+ and gets more positive
 - A neutral base becomes a **cation** after gain of H^+ $H^+ + NH_3 \rightarrow NH_4^+$
 - An anionic base becomes neutral after gain of H^+ $H^+ + OH^- \rightarrow H_2O$

The change in either charge or number of H's can help identify whether a chemical is functioning as an acid or a base.

- Every base needs a lone pair which gets used to bond to the new hydrogen
 - The two electrons involved in the new bond to hydrogen always come from an electron pair on the base



- Water can function as either a base (accepting an H^+ when an acid is placed in water) or as an acid (donating an H^+ when a base is placed in water)

5. In every acid-base reaction, you must have both an acid (a chemical functioning as the H^+ donor) and also a base (a lone-pair donating chemical functioning as the H^+ acceptor)
- An acid can't give unless there is some basic lone-pair to take.....

Terminology: H^+ = "proton"

Conjugate Acid-Base Pairs

Structures that differ by one H and one charge unit are referred to as conjugate acid-base pairs

Conjugate Acid	Conjugate Base	Conjugate Acid	Conjugate Base
HF	F^-	H_3O^+	H_2O
HCl	Cl^-	H_2O	HO^-
H_2SO_4	HSO_4^-	NH_4^+	NH_3
HSO_4^-	SO_4^{2-}		

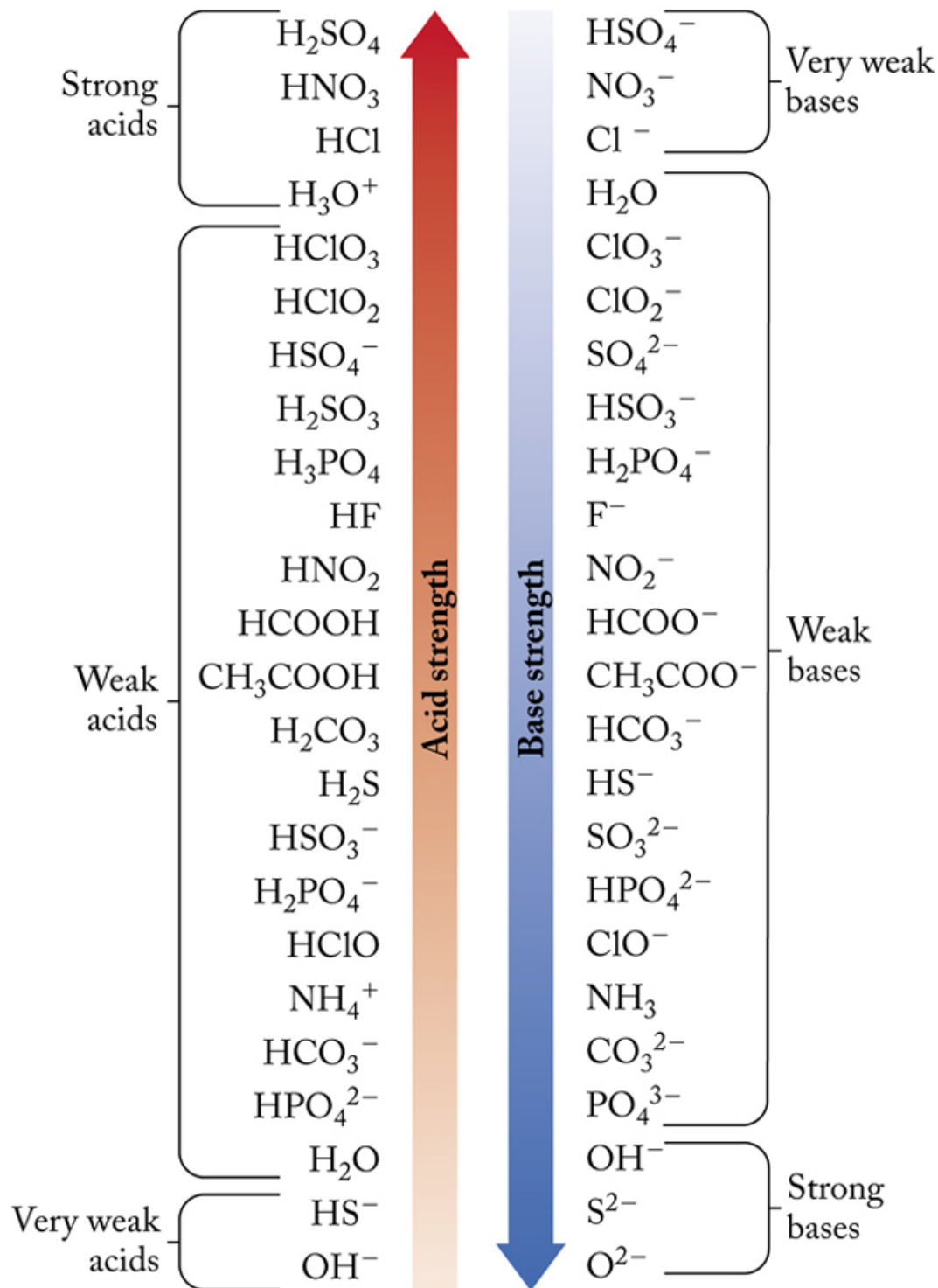
1. Draw the conjugate bases	2. Draw the conjugate acids
a. HCN	a. SO_4^{2-}
b. HBr	b. NH_3
c. CH_4	c. Cl^-

Relative Strengths of Acids and Bases

	Acid	Base		
Strong acids, 100% Ionized in H_2O	HCl H_2SO_4	Cl^- HSO_4^- H_2O	Nonbases	
	H^+ (aq) = H_3O^+ HSO_4^- HF H_2CO_3	SO_4^{2-} F^- HCO_3^-		
	NH_4^+ HCO_3^- H_2O	NH_3 CO_3^{2-} OH^-		
Nonacids	OH^- H_2	O^{2-} H^-		Strong bases, 100% Protonated in H_2O

- Stronger acids have weaker conjugate bases and weaker acids have stronger conjugate bases
- Stronger bases have weaker conjugate acids and weaker bases have stronger conjugate acids

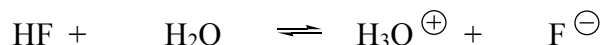
Relative Strength of Acids and Bases



Chemistry: The Science in Context 3/e Figure 17.4
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Conjugate Pairs in Acid-Base Reactions and Acid-Base Equilibria

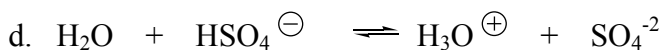
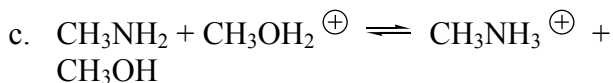
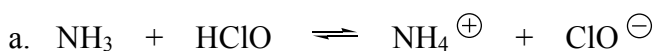
- Note: Some acid-base reactions go entirely to the product side, or stay entirely on left side
- But many acid-base reactions involve equilibria, in which a proton is shuffling back and forth from side to side
- In the example shown, a proton (H^{\oplus}) jumps back and forth between F and O.
 - Going from left to right, F is the giver ($\text{HF} = \text{acid}$) and O the acceptor ($\text{H}_2\text{O} = \text{base}$)
 - Returning from right back to left, O is the giver ($\text{H}_3\text{O}^{\oplus} = \text{acid}$) and F the acceptor ($\text{F}^{\ominus} = \text{base}$)

Notes

- Each side of every acid-base reaction has one thing that functions as an acid and the other as a base. (This is true on the right side as well as on the left side).
- Every acid-base reaction has 2 conjugate pairs
 - For the acid on the left, it's conjugate base appears on the right side
 - For the base on the left, it's conjugate acid appears on the right side.

Problems: For each of the species in the following equilibria, mark whether it functions as an acid or a base?

- For each of the species in the following equilibrium, draw an arrow to it's conjugate.

Notes/Notice:

- Notice the change in H-count and the change in charge for each of these
- The acid on the left always loses a hydrogen and becomes one step unit more negative
- The base on the left always gains a hydrogen and becomes more positive
- Cations usually function as acids**
 - They are positive, and want to get rid of H^{\oplus} to alleviate positive charge
- An anion usually function as a base**
 - It usually wants to get more positive, and the negative charge always means it has a lone-pair available
 - Some exceptions, such as example "d"

Acid/Base Strength

1. **Strong acids** are better H^{\oplus} donors than **weaker acids**

Strong bases are better H^{\oplus} acceptors than weaker bases

2. Acid/base strength depends on love for H^{\oplus}

• Consider the conjugate pair of Z^{\ominus} and HZ

a. High H^{\oplus} Love: Suppose Z^{\ominus} really loves H^{\oplus}

1. Then Z^{\ominus} is a strong base

• It aggressively grabs H^{\oplus} from somebody else

2. Then HZ is a very weak acid or a total non-acid

• Z tightly holds onto the H^{\oplus}

• It doesn't let anybody else steal H^{\oplus} unless it's a base who loves H^{\oplus} even more

b. Low H^{\oplus} Love: Suppose Z^{\ominus} doesn't have much love for H^{\oplus}

1. Then Z^{\ominus} is a weak base or a totally non-base

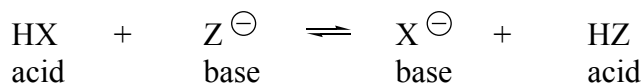
• It's very weak about grabbing H^{\oplus} from somebody else

2. Then HZ is acidic

• Z is very weak about holding onto the H^{\oplus}

• Some base who loves H^{\oplus} more can easily steal the H^{\oplus} away and leave Z^{\ominus} behind

3. Love for H^{\oplus} and the Competition between Competing Bases



NOTICE: There is one hydrogen, but two things (Z^{\ominus} and X^{\ominus}) competing for it.

a. Whichever base loves H^{\oplus} **more** will be the **stronger base**, and the equilibrium will drive to the opposite direction \rightarrow to the conjugate acid of the strong base

b. Whichever base loves H^{\oplus} **less** will lose the competition and remain in its basic form

1. Strong love for H^{\oplus} = strong base

2. Equilibrium goes from strong base to weak base, favors the side where the weaker base lies.

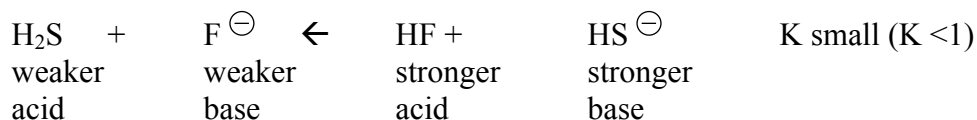
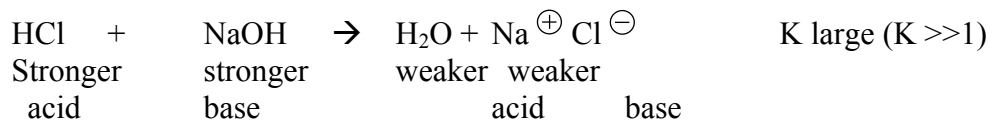
3. In the same way, the equilibrium always goes from the stronger acid to the weaker acid, and always favors the side with the weaker acid

4. The weaker acid and weaker base are always on the same side, and the stronger acid and stronger base are always together on the other side

4. Acid-Base Strength and the Direction of Acid-Base Equilibria

*Acid/base reactions always go from <u>stronger</u> acid/base to weaker <u>acid</u> + <u>base</u>
--

K favors weaker



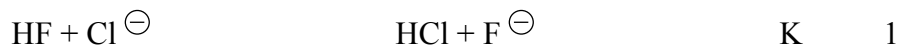
- Stronger acid + base always on same side
- If you know any of relative strengths, can predict sense, K
- If given K info, can identify weaker/stronger

Problems

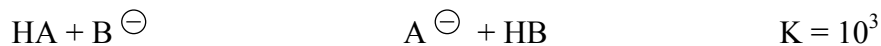
- HF is stronger than HNO_2 . Predict the “direction” of the reaction, and say whether K will be greater or less than 1. (ID each as acid or base)



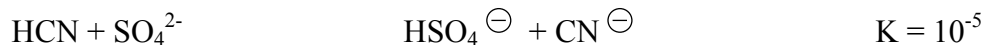
- Predict the “direction” of the reaction, and say whether K will be greater or less than 1.



- Classify each as the weaker or stronger acid or base.



- Classify each as the weaker or stronger acid or base.



5. Direct Relationship between strengths of conjugate acid/base

<u>Acid Strength</u>	<u>Strength of Conjugate Base</u>
Strong	Nonbasic
Weak	Weak
Nonacid	Strong base

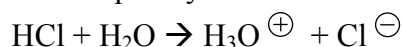
Note: there is a huge range of strengths within the “weak” category

	Acid	Base		
Strong acids, 100% Ionized in H ₂ O	HCl H ₂ SO ₄	Cl [⊖] HSO ₄ [⊖]	Nonbases	
	H [⊕] (aq) = H ₃ O ⁺ HSO ₄ ⁻ HF H ₂ CO ₃	H ₂ O SO ₄ ²⁻ F [⊖] HCO ₃ [⊖]		
	NH ₄ [⊕] HCO ₃ [⊖] H ₂ O	NH ₃ CO ₃ ²⁻ OH [⊖]		
Nonacids	OH [⊖] H ₂	O ²⁻ H [⊖]		Strong bases, 100% Protonated in H ₂ O

<p>The weaker the acid, the stronger it's conjugate base The stronger the acid, the weaker it's conjugate base</p>
--

6. Strong Acids versus Weak Acids versus Nonacids. How do they Differ in Water?

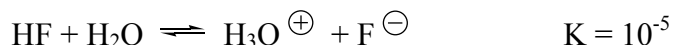
a. **Strong acids** ionize completely in water



- There is **NO** acid left, no acid where the H and the Cl are bonded.
- Goes completely to the product side.

b. **Weak acids** ionize incompletely in water

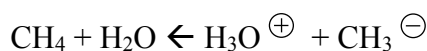
- An equilibrium exists
- Normally only a small amount of product ion is present at equilibrium, and most of the weak acid is in its undissociated form



- There is plenty of HF left. But meaningful amounts of H₃O[⊕] + F[⊖] ions present.
- Some “weak” acids are stronger or weaker than others.

c. **Nonacids:** Don't ionize at all in water.

- No equilibrium exists
- Stays completely on the left side



17.1 Recognizing Acids

1) **Memorize Six strong acids**

HCl HBr HI HNO₃ H₂SO₄ HClO₄

- **Assume all other acids are weak acids**
- The conjugate anions of these strong acids are nonbasic

2) Weak acids

a. Usually formula written with H in front

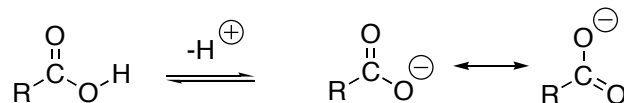
HF HCN H₂S H₂CO₃ → acids

CH₄

NH₃ SiH₄ → nonacids

*** Note: NOT ALL H's are acidic!!**

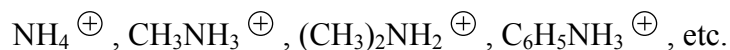
b. Carboxylic acids (RCOOH, where R is generic for almost anything)



- The “R” group can be anything, but is usually hydrocarbon
- The anion is stabilized by resonance
- Carboxylic acids are often written as: CH₃COOH, C₂H₅COOH, etc.

c. Ammonium Ions are weak acids (see more under bases, amines)

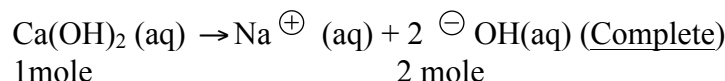
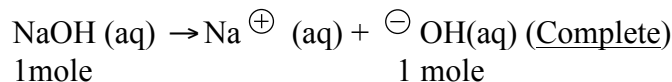
- Conjugate acids of neutral amine bases
- Formal positive charge on nitrogen
- Unlike most acids, these are cationic species



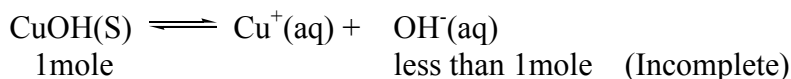
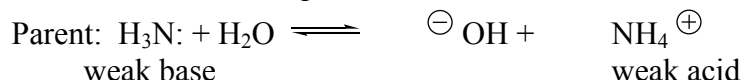
Recognizing Bases1. Soluble metal hydroxides \Rightarrow strong bases

- All **Group 1 metal hydroxides, many Group 2...**
- Group 1 metal hydroxides produce 1 mole of hydroxide per mole of formula
- Soluble Group 2 metal hydroxides produce 2 moles of hydroxide per formula

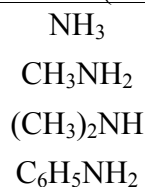
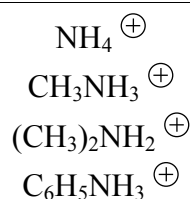
Group 1	Group 2
LiOH, NaOH, KOH ...	Ca(OH) ₂ , Ba(OH) ₂ ...



- most Transition-metal hydroxides have limited solubility and aren't effectively strong

2. Amines: Neutral N Compounds \Rightarrow weak bases

- Other amines have N: in common, but replace one or more of the hydrogens with other thing, usually carbon groups

Amines Bases (examples)Conjugate acids = "Ammonium" Ions

- N lone pairs accept H[⊕]
- Amines are the only "neutral bases". All other bases have anionic charge.
- The conjugate acids are called "ammonium ions" (see earlier)
 - "Amines" = neutral, weakly basic
 - "Ammoniums" = cationic, weakly acidic
- The ammonium ions have formal [⊕] charge on N

3. Any conjugate base of a weak acid is weak base

4. Any conjugate base of a non-acid is a strong base

5. Any conjugate base of a strong acid is a non base

Note: Most Anions are Basic. Whenever you see an anion, consider whether it will be basic!

6. Evaluating the Basicity of Anions

- Draw the conjugate acid of the anion
- Evaluate the acidity of the conjugate "acid" as strongly acidic, weakly acidic, or nonacidic
- Based on the acidity of the acid, decide what the strength of the anion base would be.

<u>Conjugate Acid Strength</u>	<u>Strength of Conjugate Base</u>
Strong acid	Nonbasic
Weak acid	Weak Base
Non-acid	Strong base

<u>Base Strength</u>	<u>Anion</u>	<u>Conjugate Acid</u>	<u>Acid Strength</u>
	F^{\ominus}	HF	
	CN^{\ominus}	HCN	
	$H_2PO_4^{\ominus}$	H_3PO_4	
	Cl^{\ominus}	HCl	
	H^{\ominus}	H_2	
	CH_3^{\ominus}	CH_4	

Note: Most anions are basic

- Memorize the six anions derived from strong acids that are not basic
- Assume any other anion is basic

Six strong Acids HCl HBr HI HNO_3 H_2SO_4 $HClO_4$

Six Non-Basic Anions Cl^{\ominus} Br^{\ominus} I^{\ominus} NO_3^{\ominus} HSO_4^{\ominus} ClO_4^{\ominus}

Recognizing and Classifying Acid/Base Character of Ionic Formulas

1. Distinguish molecular from ionic formulas

2. For ionics, check each ion separately

a. Is the cation acidic?

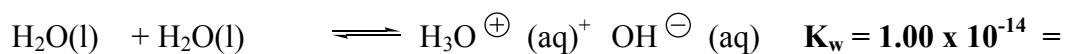
- No if it's a group 1 or group 2 metal cation
- Yes if it's a transition metal cation
- Yes if it's an ammonium cation

b. Is the anion basic?

- No if it's one of the six non-basic anions derived from strong acids
- Yes if it's any other anion

1. Classify as Strong Acid, Weak Acid, Strong Base, Weak Base, or Non-acid/base
 - a. HBr
 - b. HF
 - c. $\text{CH}_3\text{CH}_2\text{NH}_2$
 - d. $\text{CH}_3\text{CH}_2\text{COOH}$
 - e. H_2SO_4
 - f. H_3PO_4
 - g. HClO
 - h. ClO^\ominus
 - i. Cl^\ominus
 - j. NO_3^\ominus
 - k. O^{2-}
 - l. CH_4
 - m. NaOH
 - n. NaF
 - o. KCl
 - p. NH_4NO_3
 - q. FeBr_3

Autoionization of water (17.2). pH and pOH



1. Water is both weakly acidic and basic
2. Amount of ions is teensy but very important
3. $K_w = 1.00 \times 10^{-14}$ always true
4. If either $[\text{H}_3\text{O}^\oplus]$ or $[\text{OH}^\ominus]$ known, can calculate other

$[\text{H}_3\text{O}^\oplus][\text{OH}^\ominus] = 1.00 \times 10^{-14}$ Memorize!
--

Neutral: $[\text{H}_3\text{O}^{\oplus}] = 1 \times 10^{-7} = [\text{OH}^{\ominus}]$ pH = 7 Acidic: $[\text{H}_3\text{O}^{\oplus}] > 1 \times 10^{-7} > [\text{OH}^{\ominus}]$ pH < 7 Basic: $[\text{H}_3\text{O}^{\oplus}] < 1 \times 10^{-7} < [\text{OH}^{\ominus}]$ pH > 7	Note: H^{\oplus} vs. $\text{H}_3\text{O}^{\oplus}$ <ul style="list-style-type: none"> H^{\oplus} (proton) in water exists as $\text{H}_3\text{O}^{\oplus}$ (hydronium). But H^{\oplus} is easier to write! They are really the same thing.
---	--

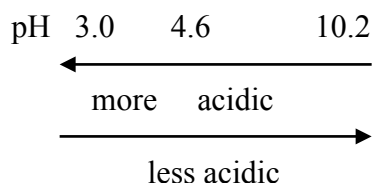
The pH Scale (17.2)

$\text{pH} = -\log[\text{H}_3\text{O}^{\oplus}]$	$[\text{H}_3\text{O}^{\oplus}] = 10^{-\text{pH}}$	Much nicer numbers
--	---	--------------------

On calculator: enter $[\text{H}^{\oplus}]$, hit “log”, and correct the sign from negative to positive

On calculator: enter pH, switch the sign from positive to negative, and hit 10^x button (depending on calculator)

- Higher numbered pH \rightarrow less H^{\oplus} , less acidic, more basic
Lower numbered pH \rightarrow more H^{\oplus} , more acidic, more less⁺



- pH = 7 neutral pH < 7 acidic pH > 7 basic
- pH change of 1 = tenfold change in $[\text{H}^{\oplus}]$
Change of 2 = 100-fold change
pH change of 8 \rightarrow 4 isn't double the acid or half the acid, it's 10 thousand times more!
- Number of significant figures in $[\text{H}^{\oplus}]$ = number of digits after decimal in pH

$$[\text{H}^{\oplus}] = 3.6 \times 10^{-6} \rightarrow \text{pH} = 5.44$$

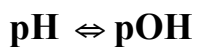
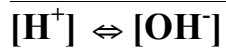
2 sig fig \rightarrow 2 after decimal

- Small pH changes \rightarrow death
 - $7.35 < \text{blood} < 7.45$
 - bio rates are often strongly H^{\oplus} catalyzed, with 2nd or 3rd order rate dependence on $[\text{H}^{\oplus}]$

6. $\text{pOH} = -\log[\text{OH}^-]$ just like $\text{pH} = -\log[\text{H}^{\oplus}]$	$[\text{OH}^-] = 10^{-\text{pOH}}$ just like $[\text{H}^{\oplus}] = 10^{-\text{pH}}$
--	---

- Since $10^{-14} = [\text{H}^{\oplus}][\text{OH}^-] \rightarrow$ take negative log of both sides \rightarrow **14.00 = pH + pOH**

Skills: interconvert among



To know any one allows you to find any of the others!

Problems

1. Find pH for following

a. $[\text{H}_3\text{O}^+] = 1.0 \times 10^{-4}$

b. $[\text{H}^+] = 1.0 \times 10^{-11}$

c. $[\text{H}^+] = 3.2 \times 10^{-4}$

d. $[\text{OH}^-] = 1.0 \times 10^{-8}$

e. $[\text{OH}^-] = 5.8 \times 10^{-4}$

f. $\text{pOH} = 8.30$

2. Find pOH:

a. $[\text{H}^+] = 3.9 \times 10^{-5}$

b. $[\text{OH}^-] = 3.9 \times 10^{-5}$

c. $\text{pH} = 3.95$

3. Find both

$[\text{H}^+]$

$[\text{OH}^-]$

a. $\text{pH} = 3.72$

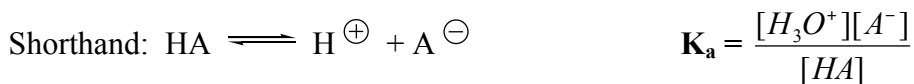
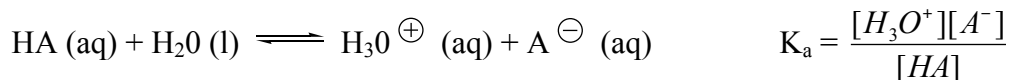
b. $\text{pH} = 9.81$

c. $[\text{H}^+] = 3.5 \times 10^{-8}$

d. $[\text{OH}^-] = 4.1 \times 10^{-3}$

Equilibrium Expressions and Ionization Constants for Acids, Bases. (17.3)

A. Acids



- Strong acids: ionize completely ($K_a = \text{infinity}$)
- Weak acids: $K_a < 1$
- Larger $K_a \Rightarrow$ stronger acid Smaller $K_a \Rightarrow$ weaker acid
- For weak acids, ionizations may be minimal but is still significant
 - for math calculations, the “simplifying assumption” is usually useful
- Since A^{\ominus} and HA are conjugates:
 - larger $K_a \Rightarrow$ less basic A^{\ominus} (stronger acid \rightarrow weaker base)
 - smaller $K_a \Rightarrow$ more basic A^{\ominus} (weaker acid \rightarrow stronger base)

B. Bases

Generic	$\text{Base(aq)} + \text{H}_2\text{O(l)} \rightleftharpoons \text{OH}^{\ominus} \text{ (aq)} + \text{Base-H}^{\oplus} \text{ (aq)}$ <p style="text-align: center;">Conjugate acid</p>	$K_b = \frac{[\text{OH}^{\ominus}][\text{BH}^{\oplus}]}{[\text{B}]}$
Anionic Base	$\text{A}^{\ominus} + \text{H}_2\text{O} \rightleftharpoons \text{OH}^{\ominus} + \text{HA}$ <p style="text-align: center;">Conjugate acid</p>	$K_b = \frac{[\text{OH}^{\ominus}][\text{HA}]}{[\text{A}^{\ominus}]}$
Neutral Amine Base	$\text{NH}_3 + \text{H}_2\text{O} \rightleftharpoons \text{OH}^{\ominus} + \text{NH}_4^{\oplus}$ <p style="text-align: center;">Amine Ammonium</p>	$K_b = \frac{[\text{OH}^{\ominus}][\text{NH}_4^{\oplus}]}{[\text{NH}_3]}$

16.7 Calculations involving K_a , K_b , pH, pOHA. **Strong Acids:** $[\text{HA}] = [\text{H}^{\oplus}] \Rightarrow$ pH

- Complete ionization $\text{HCl} \rightarrow \text{H}^{\oplus} + \text{Cl}^{\ominus}$
- To know the concentration of the strong acid is to know the concentration of H^{\oplus}

B. **Strong Bases:** complete formation of OH^{\ominus}

- $[\text{NaOH}] = [\text{OH}^{\ominus}] \Rightarrow$ pOH, pH
 - for a group one metal hydroxide (NaOH, etc.), you get exactly as many moles of hydroxide as you put in of NaOH, and $[\text{NaOH}] = [\text{OH}^{\ominus}]$
 - $\text{NaOH} \rightarrow \text{Na}^{\oplus} + \text{OH}^{\ominus}$
- For a group two metal hydroxide, you get two moles of hydroxide for every one mole of formula that you put in.
 - $1 \text{ Ba(OH)}_2 \rightarrow 1 \text{ Ba}^{2+} + 2 \text{ OH}^{\ominus}$
 - $[\text{OH}^{\ominus}] = 2 ([\text{Ba(OH)}_2])$
- Since $[\text{OH}^{\ominus}]$ is knowable, you can then plug in, and find pOH, pH, and/or $[\text{H}^{\oplus}]$

Some pH Calculations Involving Strong Acids or Bases

1. What is the pH of 1.36×10^{-3} M H_2SO_4 ?
2. An HCl solution has pH = 2.16. what is [HCl]?
3. What is pH for 0.013 M KOH solution?
4. What is pH for a solution that is 0.013 M in $\text{Ca}(\text{OH})_2$?
5. What is the pH if 22 g of $\text{Ba}(\text{OH})_2$ (90 g/mol) is dissolved in 760 mL of water?

C. Weak Acids Calculation: Equilibrium, K_a , and pH ICE-able (Section 17.3)

Two Key Equations	$K_a = \frac{[\text{H}^+]^2}{[\text{HA}]_{\text{init}}}$	$[\text{H}^+] = \sqrt{K_a \cdot [\text{HA}]}$
-------------------	--	---

1. **Major Application 1:** Given a known K_a , Solve for pH When a Known Amount of Weak Acid is Placed in a Known Amount of Water

Logic: Use $K_a \rightarrow$ solve for $[\text{H}^{\oplus}] \rightarrow$ solve for pH

Steps

1. Whether it's given in molarity or not, convert the sample/solvent ratio into Molarity
2. Set up an ICE table
3. Solve for equilibrium $[\text{H}^{\oplus}]$
 - Use simplifying assumption if K_a is reasonably small
 - Use another simplifying assumption that the original population of H^{\oplus} is also reasonably small relative to the final, equilibrium amount of H^{\oplus}
4. Use $[\text{H}^{\oplus}]$ to solve for pH

- | |
|---|
| 5. Or: If K_a is small enough so that the simplifying assumption is reasonable, you can directly plug into the equation shown above |
|---|

	HA	\rightleftharpoons	H [⊕]	+	A [⊖]
Initial	[HA] _{init}		1.0 x 10 ⁻⁷		0
Change					
Equilibrium					
Equilibrium After Simplifying Assumptions					

$K_a =$

When is simplifying assumption safe? Use the >100K rule:	If $\frac{[HA]_{init}}{K_a} > 100 \rightarrow$ simplifying assumption is safe
---	---

When the simplifying assumptions are used:

$$K_a = \frac{[H^+]^2}{[HA]_{init}}$$

$$[H^+] = \sqrt{K_a \times [HA]_{init}}$$

When the first simplifying assumption is not used (but the second one is)

$$K_a = \frac{[H^+]^2}{[HA]_{init} - [H^+]}$$

[H[⊕]] requires a quadratic solution

2. **Major Application 2:** Given a measured pH, Solve for K_a When a Known Amount of Weak Acid is Placed in a Known Amount of Water

Logic: Use pH \rightarrow solve for [H[⊕]] \rightarrow solve for K_a

$$K_a = \frac{[H^+]^2}{[HA]_{init}}$$

Weak Acid pH/ K_a Problems

1. pH \rightarrow K_a What is K_a for an acid if an 0.15 M solution is prepared and found to have pH = 4.86?

Logic:

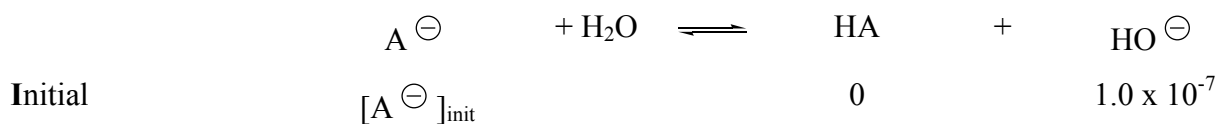
2. $K_a \rightarrow \text{pH}$ What is pH for a 0.15 M solution of an acid with $K_a = 2.2 \times 10^{-6}$?

Logic:

3. If an 0.23 M solution of an acid gives $\text{pH} = 3.82$, what is K_a for acid?

4. If a 0.11 M solution has a $K_a = 1.3 \times 10^{-8}$ acid, what is pH?

D. Weak Base Calculations involving K_b and pH (Section 17.3)



Change

Equilibrium

**Equilibrium
After Simplifying
Assumptions**

$K_b =$

When is simplifying assumption safe? Use the >100K rule:	If $\frac{[\text{base}]_{\text{init}}}{K_b} > 100 \rightarrow$ simplifying assumption is safe
---	---

When the simplifying assumptions are used:

$$K_b = \frac{[\text{HO}^-]^2}{[\text{A}^-]_{\text{init}}}$$

$$[\text{HO}^\ominus] = \sqrt{K_b \times [\text{A}^-]_{\text{init}}}$$

When the first simplifying assumption is not used but the second one is

$$K_b = \frac{[\text{HO}^-]^2}{[\text{A}^-]_{\text{init}} - [\text{HO}^-]}$$

$[\text{HO}^\ominus]$ requires a quadratic solution

Applications

1. $\text{pH} \rightarrow K_b$

Strategy: $\text{pH} \rightarrow \text{pOH} \rightarrow [\text{HO}^\ominus] \rightarrow K_b$

2. $K_b \rightarrow \text{pH}$

Strategy: $K_b \rightarrow [\text{HO}^\ominus] \rightarrow \text{pOH} \rightarrow \text{pH}$

Problems: pH and K_b

1. $\text{pH} \rightarrow K_b$ What is K_b if a 0.123 M solution of a weak base gives $\text{pH}=10.62$?

2. $K_b \rightarrow \text{pH}$ If K_b for a weak base is 1.6×10^{-5} , what is the pH of a 0.222 M solution of the base?

E. Relationship Between K_a and K_b for Conjugate acids/bases (Section 16.7, p 794)

- Review: stronger the acid, weaker the conjugate base (and vice versa)

$$\boxed{K_a \times K_b = 1.0 \times 10^{-14}}$$

Review Table 16.2

- Given one, can solve for other.
- Tables routinely provide only one; expect you to solve for other
- Can rank relative strengths of acids(or bases) given info about conjugates
- Toughest problem: given K_a for conjugate acid, calculate pH for a solution of weak base
 - Logic: $K_a \rightarrow K_b \rightarrow [HO^\ominus] \rightarrow pOH \rightarrow pH$

Derivation of $K_a K_b = 10^{-14}$ (not responsible for derivation, just for interest)

$$K_a = \frac{[H_3O^+][A^-]}{[HA]}$$

$$K_b = \frac{[OH^-][HA]}{[A^-]}$$

$$\text{So } K_a K_b = \left(\frac{[H_3O^+][A^-]}{[HA]} \right) \frac{[OH^-][HA]}{[A^-]} = [H_3O^+][OH^-] = 1.0 \times 10^{-14} \quad \text{Thus } K_a K_b = K_w = 10^{-14}$$

<u>Acid Strength</u>	<u>K_a</u>	<u>K_b</u>	<u>Strength of Conjugate Base</u>
Strong	$K_a > 1$	$K_b < 1 \times 10^{-14}$	Nonbasic
Weak	$1 \times 10^{-14} < K_a < 1$	$1 \times 10^{-14} < K_b < 1$	Weak
Nonacid	$K_a < 1 \times 10^{-14}$	$K_b > 1$	Strong base

Problems Involving Relationship between K_a and K_b for Conjugated Acid/Base

Substance	HF	HN ₃	HCN
K_a	6.8×10^{-4}	1.9×10^{-3}	4.9×10^{-10}
Relative Acidity			
Conjugate Base			
Relative Basicity			
K_b			

- Rank the acidity for the three weak acids, 1 being strongest.
- Rank the basicity, 1 being the strongest, for: NaCN NaF NaN₃

Substance	HF	HN ₃	HCN
K _a	6.8×10^{-4}	1.9×10^{-3}	4.9×10^{-10}
Conjugate Base			
K _b			

3. What is K_b for N₃⁻?

4. What is pH for a solution that is 0.12 M in NaF⁻?

Logic:

5. What is pH for a solution that is 0.20 M in NaCN?

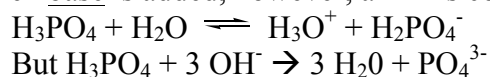
Logic:

Polyprotic Acids: More than One H⁺ Available (Section 17.4)H₂SO₄, H₃PO₄, H₂CO₃,...

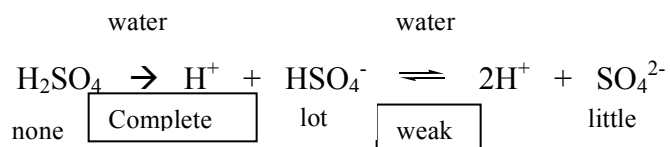
1. Each H⁺ gets successively **less** acidic (by > 1000)

Relative Acidity	Acid		Conjugate Base	Relative Basicity
	H ₃ PO ₄	K _{a1} = 10 ⁻³	H ₂ PO ₄ ⁻	
	H ₂ PO ₄ ⁻	K _{a2} = 10 ⁻⁸	HPO ₄ ²⁻	
	HPO ₄ ⁻²	K _{a3} = 10 ⁻¹³	PO ₄ ³⁻	

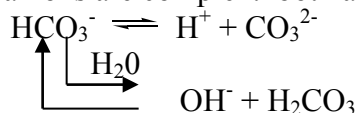
2. As acids in water, only consider the first ionization.
 3. When base is added, however, all H⁺'s come off (stoichiometry permitting)



4. H₂SO₄: 1st strong, 2nd weak



5. Some anions are complex: both acidic and basic!!

**Polyprotic Acid/Base Problems**

1. Which is the stronger acid?



2. Which is the stronger base?



Polyprotic Acids: Each H becomes less acidic

TABLE 17.6 Ionization Equilibria for Two Triprotic Acids		
Phosphoric Acid		
(1)	$\text{HO}-\text{P}(\text{OH})_2 \rightleftharpoons \text{HO}-\text{P}(\text{OH})(\text{O}^-) + \text{H}^+$	$K_{a_1} = 7.11 \times 10^{-3}$
(2)	$\text{HO}-\text{P}(\text{OH})(\text{O}^-) \rightleftharpoons \text{O}^--\text{P}(\text{OH})(\text{O}^-) + \text{H}^+$	$K_{a_2} = 6.32 \times 10^{-8}$
(3)	$\text{O}^--\text{P}(\text{OH})(\text{O}^-) \rightleftharpoons \text{O}^--\text{P}(\text{O}^-)_2 + \text{H}^+$	$K_{a_3} = 4.5 \times 10^{-13}$
Citric Acid		
(1)	$\text{HO}-\text{C}(\text{CH}_2\text{COOH})_2 \rightleftharpoons \text{HO}-\text{C}(\text{CH}_2\text{COO}^-)(\text{CH}_2\text{COOH}) + \text{H}^+$	$K_{a_1} = 7.44 \times 10^{-4}$
(2)	$\text{HO}-\text{C}(\text{CH}_2\text{COO}^-)(\text{CH}_2\text{COOH}) \rightleftharpoons \text{HO}-\text{C}(\text{CH}_2\text{COO}^-)_2 + \text{H}^+$	$K_{a_2} = 1.73 \times 10^{-5}$
(3)	$\text{HO}-\text{C}(\text{CH}_2\text{COO}^-)_2 \rightleftharpoons \text{O}^--\text{C}(\text{CH}_2\text{COO}^-)_2 + \text{H}^+$	$K_{a_3} = 4.02 \times 10^{-7}$

Chemistry: The Science in Context 3/e Table 17.6
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Acid-Base Properties of Common Salts

TABLE 17.7 Acid-Base Properties of Some Common Salts			
Anion Is Derived from a	Cation Is Derived from a	pH of Aqueous Solutions	Example
Strong acid	Strong base	7	NaCl
Strong acid	Weak base	<7	NH ₄ Cl
Weak acid	Strong base	>7	NaF
Weak acid	Weak base	Depends on relative values of p <i>K</i> _a and p <i>K</i> _b	p <i>K</i> _a < p <i>K</i> _b , acidic; NH ₄ F p <i>K</i> _b > p <i>K</i> _a , basic; NH ₄ HCO ₃ p <i>K</i> _a = p <i>K</i> _b , neutral; CH ₃ COONH ₄

Chemistry: The Science in Context 3/e Table 17.7
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Acid-Base Properties of Salts (Ionic Compounds) (Section 17.6)

NH ₄ Cl	MgBr ₂	NaCN
pH<7	pH=7	pH>7
acidic	neutral	basic

Recall: “salts” formed by acid/base reactions

“salt”=ionic

Example: SA/SB	HCl + NaOH → H ₂ O + NaCl	neutral
WA/SB	HF + NaOH → H ₂ O + NaF	basic
SA/WB	HCl + NH ₃ → NH ₄ ⁺ Cl ⁻	acidic
WA/WB	HF + NH ₃ → NH ₄ ⁺ F ⁻	can't tell

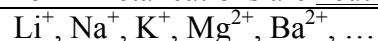
Observations:

1. Salts can be acidic, basic, or neutral.
2. Depends on strengths of acids/bases from which they form.
3. The “ions” in the salts are conjugates; may be acidic or basic!!

A. General Logic to Predict: Identify Ions individually. Check Cation, then Anion.

1. Cations: acidic or neutral

a. Group I or II metal cations are neutral

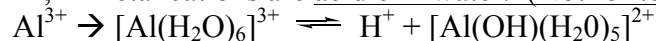


No impact on pH

b. Ammoniums are acidic



c. Al³⁺, T-metal cations are acidic in water. (Not for test)

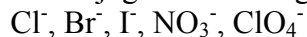


Weak acid

For test purpose, assume metal cations are neutral, ammonium cations acidic

2. Anions: basic or neutral

a. Neutral: conjugates of strong acids



b. basic: conjugates of weak acids (or non acids)



3. “Amphoteric” anions derived from polyprotic acids: can be acidic or basic

-not test responsible

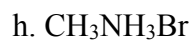
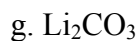
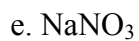


B. Predicting acidic/neutral/basic (qualitatively)

Cation	anion	salt solution	example
Neutral	neutral	neutral	NaCl, KNO ₃
Acidic	neutral	acidic	NH ₄ Cl, Fe(NO ₃) ₃
Neutral	basic	basic	NaF, K(ClO)
Acidic	basic	can't predict (without K's)	NH ₄ F, Fe(N ₃) ₃

Predicting Acid/Base Character for Ionic Formulas

1. Predict as acidic, basic, neutral, or can't tell.



2. Rank the following in terms of increasing pH, 1 being the lowest. (ID as strong/weak acid, strong/weak base, or neutral first!)



Molecular Structure and Acid/Base Strength (17.5)

- Why is something strong or weak? Acidic or Basic? Can we predict from structure, without K_a 's?

A. Key Factors on Acid Strength

1. Stability of conjugate A^- and Electronegativity*****

- Think Anion!
- Think electronegativity and -electron love

2. H-A bond strength: stronger \rightarrow less acidic

- Why H-F (strong bond) is weak acid, but H-Cl, H-Br, H-I are strong acids
- Row 2 bonds (H-F, O-H, N-H, C-H) usually stronger than row 3,4 analogs

3. Resonance

- For two oxyanions, one with resonance is more stable than one without

B. Practical Pattern

1. Horizontal Periodic Pattern: Acidity increase left \rightarrow right

	CH_4	NH_3	H_2O	HF
K_a	10^{-50}	10^{-32}	10^{-14}	10^{-4}

Note: e^- love, electronegativity/bond-polarity, anion stability all agree

Rank: Acidity of: SiH_4 SH_2 HCl PH_3

2. Vertical Periodic Pattern: Acidity Increases Top \rightarrow Bottom

-due to decreasing H-A bond strength (even though contrary to e^- love)

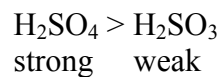
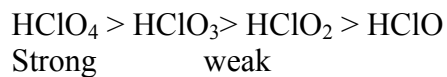
$HF < HCl$
Weak strong

$H_2O < H_2S < H_2Se$
 $K_a = 10^{-14} \quad 10^{-9} \quad 10^{-6}$

Note: Basicity of conjugates linked!!

Horizontal: $^-NH_2 > F^-$

Vertical: $F^- > Cl^-$

C. "Oxoacids": "**Extra** Oxygens's increase acidity (17.5)

Why? Extra electron-loving oxygen

1. Stabilizes resulting anion
2. Polarizes O-H
3. Weakens O-H

• **Any Neutral Oxoacid with ≥ 2 extra O's is a strong Acid**

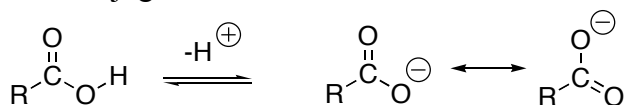
- Compare how many oxygens there are versus hydrogens

Strong: H_2SO_4 , HClO_3

weak: H_2CO_3 , H_3PO_4 , H_2SO_3

Carboxylic Acids: Famous class of oxoacids: RCOOH or RCO_2H (R is usually an H or a carbon chain.)

- Resonance stabilization of conjugate anion makes the anion more stable



Predicting Acid/Base Properties and Trends**Why?**

1. Which are acidic vs. basic vs. neutral in water?



2. Rank Acidity (1 strongest)



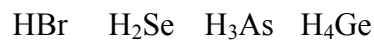
3. Rank Acidity (1 strongest)



4. Rank Acidity (1 strongest)



5. Rank Acidity (1 strongest)



6. Which would be stronger?



7. Rank Basicity (1 strongest)

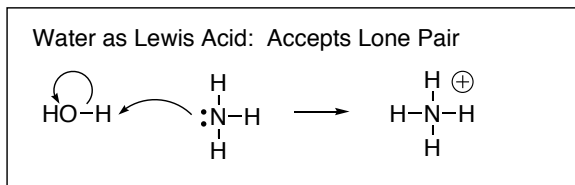
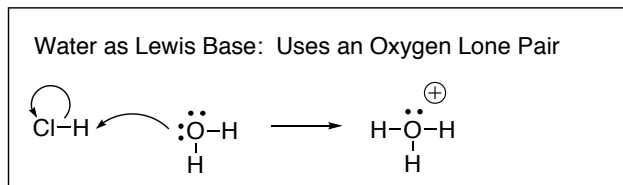


8. Rank Basicity (1 strongest)



Lewis Acids and Bases: focus on electron pairs, not H⁺ movement. (18.1)

Lewis acid: e- pair acceptor Lewis base: e- pair donor	Covers “acid-base” chemistry that doesn't involve H ⁺
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Other Examples

a.	b.
c.	d.
e.	

Notes: 1. A “base” must have a lone pair(F⁻, OH⁻, NH₃, ...)

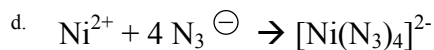
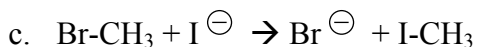
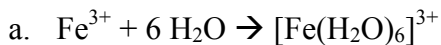
2. All anions have lone pairs → Lewis Base potential

3. An “acid” must be able to accept a lone pair

-all cations can!!

-some neutrals: BF₃, SO₂, ...Lewis Acid/Base Problems1. Which would not be a Lewis acid?

2. Identify the Lewis acid and Lewis Base



CH. 16 Acid-Base Chemistry Math Review

Key Equations, Numerical Relationships

1. $[H^+][OH^-] = 1.00 \times 10^{-14}$

2. $pH = -\log[H^+]$

$[H^+] = 10^{-pH}$ (on calculator, enter $-pH$, then punch the **10^x** button)

$pOH = -\log[OH^-]$

$[OH^-] = 10^{-pOH}$ (on calculator, enter $-pOH$, then punch the **10^x** button)

3. $pH + pOH = 14$

$pH = 14 - pOH$

Weak acid problems

$K_a = [H^+][A^-]/[HA]$

but when HA is placed in water, $[H^+] = [A^-]$ so:

When the simplifying assumptions are used:

4. $K_a = \frac{[H^+]^2}{[HA]_{init}}$

5. $[H^+] = \sqrt{K_a \times [HA]_{init}}$

When the first simplifying assumption is not used (but the second one is)

6. $K_a = \frac{[H^+]^2}{[HA]_{init} - [H^+]}$

 $[H^+]$ requires a quadratic solution

7. Quadratic Equation: for $ax^2 + bx + c = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Weak base problems

$K_b = [Base-H^+][OH^-]/[Base]$

but when Base is placed in water, $[Base-H^+] = [OH^-]$ so:

When the simplifying assumptions are used:

8. $K_b = \frac{[OH^-]^2}{[Base]_{init}}$

9. $[OH^-] = \sqrt{K_b \times [Base]_{init}}$

When the first simplifying assumption is not used but the second one is

10. $K_b = \frac{[OH^-]^2}{[Base]_{init} - [OH^-]}$

 $[OH^-]$ requires a quadratic solution

11. $K_a K_b = 10^{-14}$ for a conjugate acid/base pair.

Note: This relationship is routinely used when a K value for your acid or base is not provided, but the K value for its conjugate is. So get it indirectly.

Some Calculation Logic Scenarios

1. Strong acid \rightarrow pH

$[Strong\ acid] \rightarrow [H^+] \rightarrow pH$

2. Strong base \rightarrow pH

$[Strong\ base] \rightarrow [OH^-] \rightarrow pOH \rightarrow pH$

3. Weak acid + $K_a \rightarrow$ pH

$[Weak\ acid] + K_a \rightarrow [H^+] \rightarrow pH$

4. pH of weak acid $\rightarrow K_a$

$pH \rightarrow$ solve for $[H^+] \rightarrow K_a$

5. Weak base + $K_b \rightarrow$ pH

$[Weak\ base] + K_b \rightarrow [OH^-] \rightarrow pOH \rightarrow pH$

6. pH of weak base $\rightarrow K_b$

$pH \rightarrow$ solve for $[OH^-] \rightarrow pOH \rightarrow pH$

7. Weak base + K_a of conjugate acid \rightarrow pH

$K_a \rightarrow K_b \rightarrow [OH^-] \rightarrow pOH \rightarrow pH$

Simple Acid-Base Concept Map

